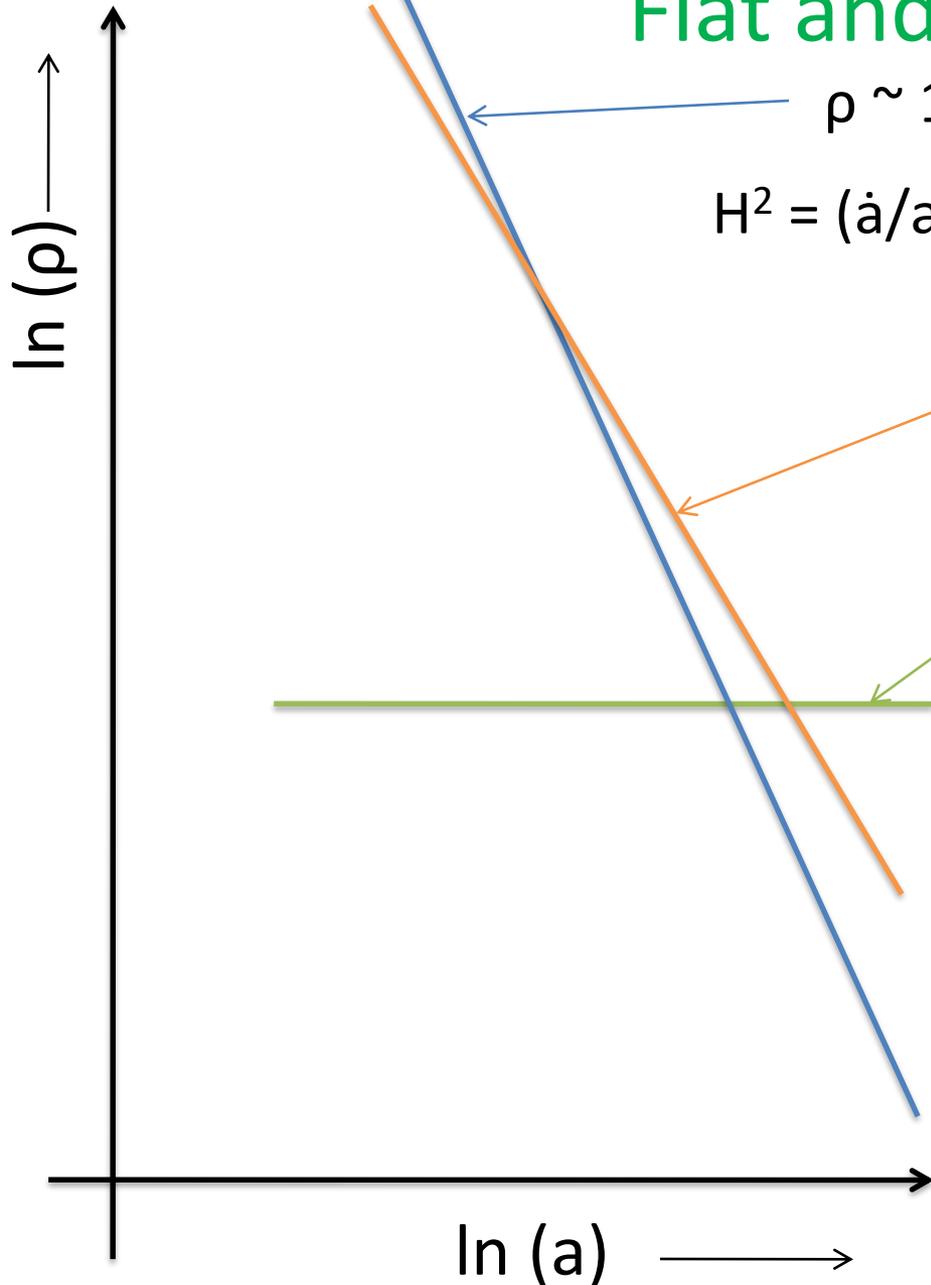


1. Cosmological parameter constraints from a large compilation of “low” redshift ($z < 8.2$) data
2. Measuring spatial curvature using CMB anisotropy and/or low redshift data

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Copernicus World Congress Tuesday 21 February 2023

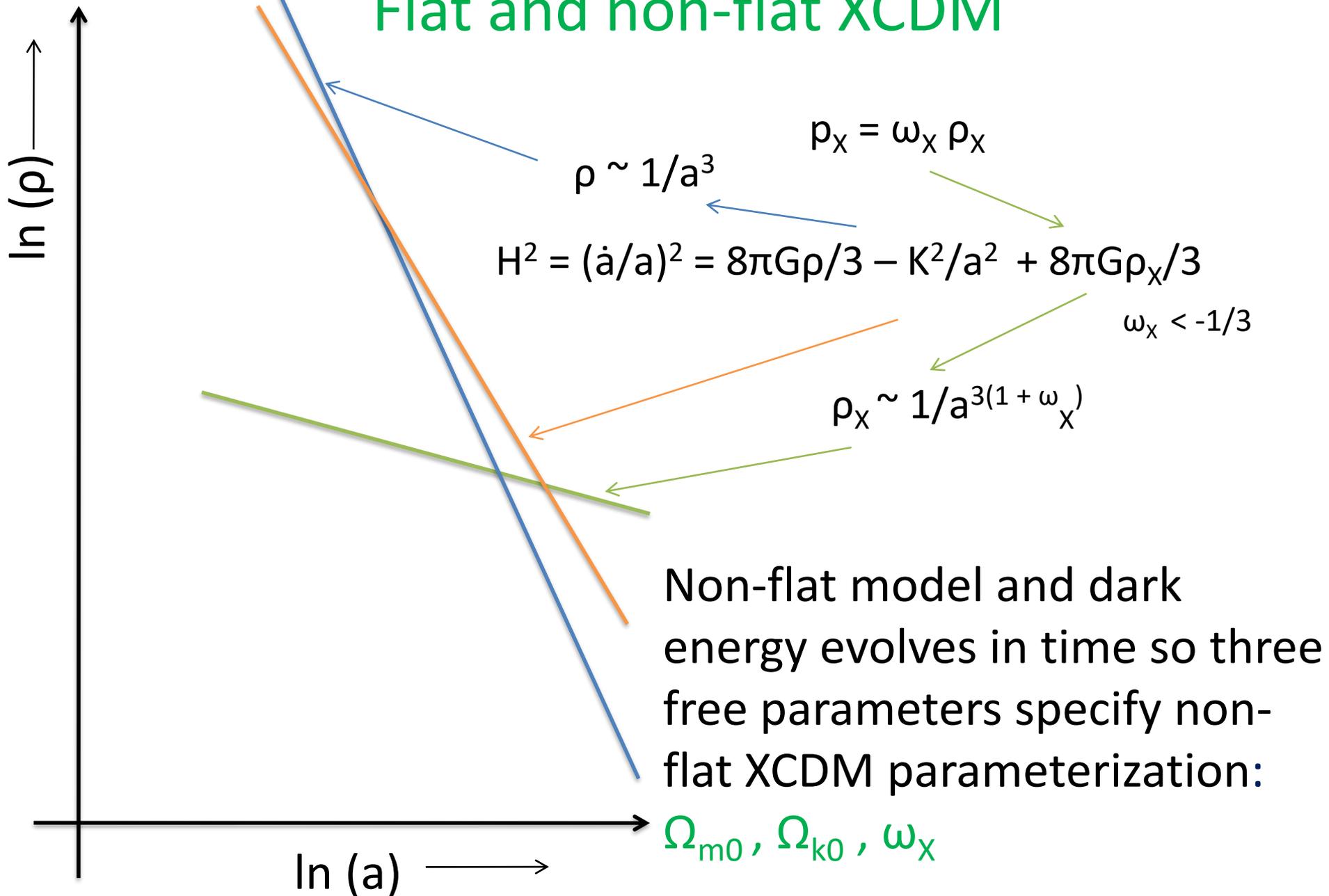
Flat and non-flat Λ CDM models



(Peebles 1984)

Non zero Ω_Λ introduces a new “fundamental” energy scale of order an meV.
(Neutrino mass?)

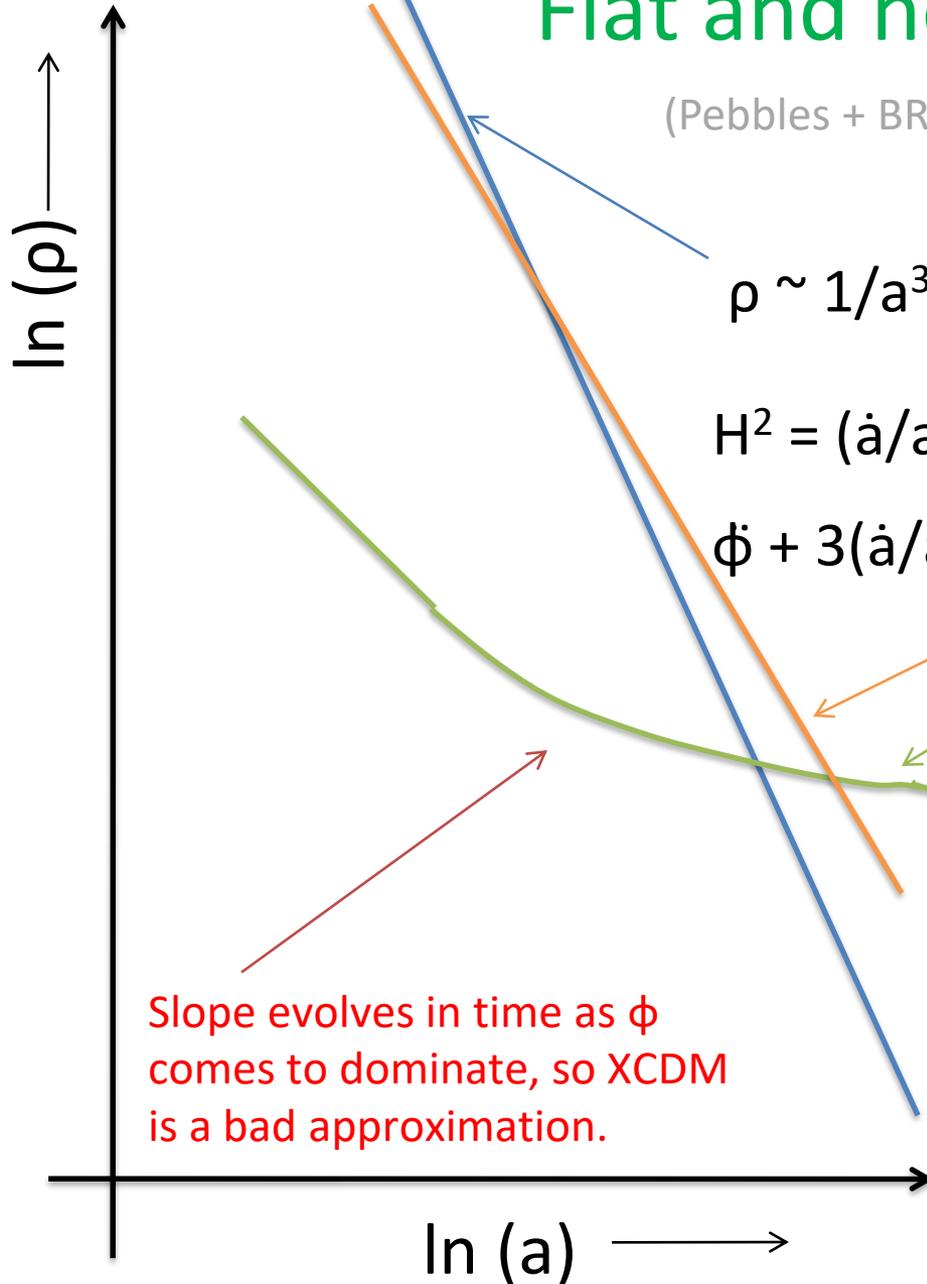
Flat and non-flat XCDM



Widely used parameterization is incomplete; arbitrarily specify $c_{sX}^2 = dp_X/d\rho_X > 0$, usually = 1.

Flat and non-flat ϕ CDM models

(Pebbles + BR 1988; Pavlov et al. PRD88, 123513 (2013))



$$\rho_\phi = (\dot{\phi}^2 + \kappa\phi^{-\alpha}/G)/2$$

$$\rho \sim 1/a^3$$

$$H^2 = (\dot{a}/a)^2 = 8\pi G\rho/3 - K^2/a^2 + 8\pi G\rho_\phi/3$$

$$\ddot{\phi} + 3(\dot{a}/a)\dot{\phi} - \kappa\alpha\phi^{-(\alpha+1)}/(2G) = 0$$

← numerically integrate

Non-flat and dark energy evolves in time so three free parameters specify non-flat ϕ CDM: Ω_{m0} , Ω_{k0} , α

Slope evolves in time as ϕ comes to dominate, so Λ CDM is a bad approximation.

ϕ CDM model is special for some $V(\phi)$: the ϕ solution is an attractor, ρ_ϕ decreases less rapidly than ρ_M and comes to dominate. This helps to partially resolve the coincidence problem and makes Λ small because the universe is old.

Hubble constant H_0 from low- z data

Measure H_0 from $z < 8.2$ BAO + $H(z)$ + SN-Pantheon + SN-DES + QSO-AS + H II G + Mg II QSO + GRB data by using cosmological models (Cao* + BR MNRAS513, 5686 (2022)) with error 2.2X Planck. Independent of CMB, since these data are also used to measure r_s (i.e., $\Omega_b h^2$ and $\Omega_c h^2$ instead of $\Omega_{m0} h^2$).

Flat Λ CDM: $(69.9 \pm 1.1) \text{ km s}^{-1} \text{ Mpc}^{-1}$

Non-flat Λ CDM: $(69.8 \pm 1.1) \text{ km s}^{-1} \text{ Mpc}^{-1}$

Flat χ CDM: $(69.7 \pm 1.2) \text{ km s}^{-1} \text{ Mpc}^{-1}$

Non-flat χ CDM: $(69.7 \pm 1.2) \text{ km s}^{-1} \text{ Mpc}^{-1}$

Flat ϕ CDM: $(69.5 \pm 1.1) \text{ km s}^{-1} \text{ Mpc}^{-1}$

Non-flat ϕ CDM: $(69.5 \pm 1.2) \text{ km s}^{-1} \text{ Mpc}^{-1}$

Independent of
cosmological model.

Closer to $(68 \pm 2.8) \text{ km s}^{-1} \text{ Mpc}^{-1}$ MS (Chen & BR PASP123, 1127 (2011))

and $(69.8 \pm 1.7) \text{ km s}^{-1} \text{ Mpc}^{-1}$ TRGB (Freedman+ ApJ919, 16 (2021))

than to $(73.04 \pm 1.04) \text{ km s}^{-1} \text{ Mpc}^{-1}$ Cepheids+SN Ia (Riess+ ApJ934, L7 (2022))

and $(67.36 \pm 0.54) \text{ km s}^{-1} \text{ Mpc}^{-1}$ CMB (Planck A&A641, A6 (2020)).

which might be interesting.

Also $\Omega_{m0} = 0.295 \pm 0.017$ with error 2.3X Planck.

*Shulei is a great student and is now looking for a US postdoc position. Thanks.

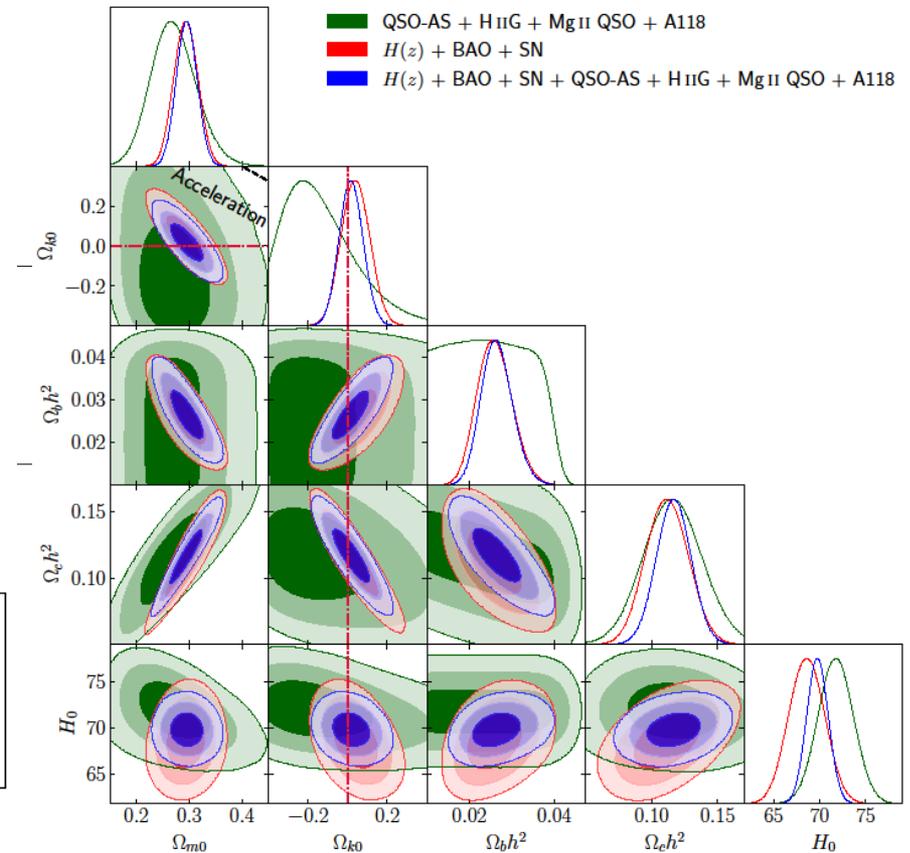
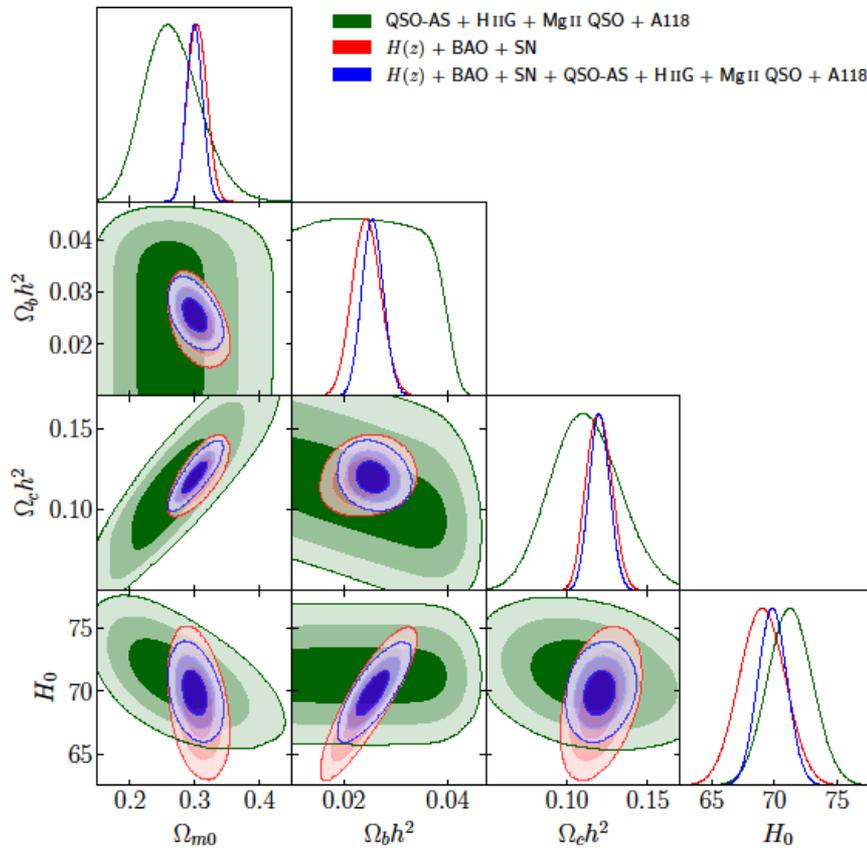
Also constrain other parameters of these six models using $z < 8.2$ BAO + $H(z)$ + SN-Pantheon + SN-DES + QSO-AS + H II G + Mg II QSO + GRB data (Cao + BR MNRAS513, 5686 (2022)).

These data give mutually consistent constraints, so can be used jointly to constrain parameters.

Do not include L_X - L_{UV} QSOs (Lusso+ A&A642, A150 (2020)) which are not standard candles (Khadka + BR MNRAS510, 2753 (2022)).

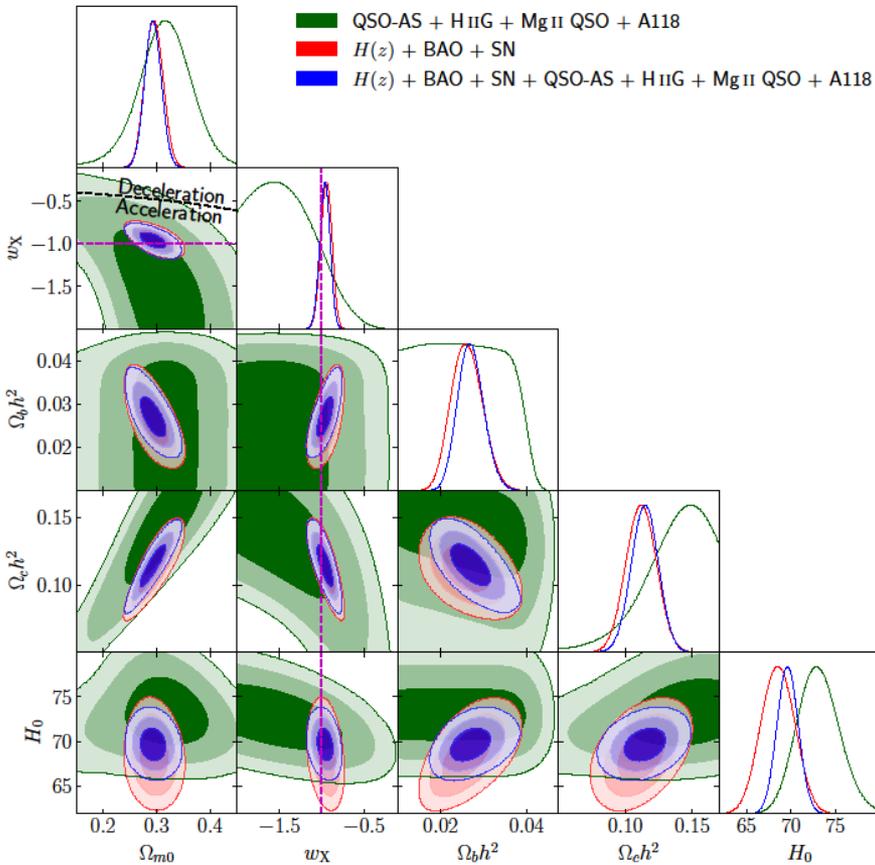
Consistent with flat geometry. Dark energy dynamics is mildly favored in both flat and non-flat ϕ CDM at 1.0-1.1 σ .

Flat and non-flat Λ CDM

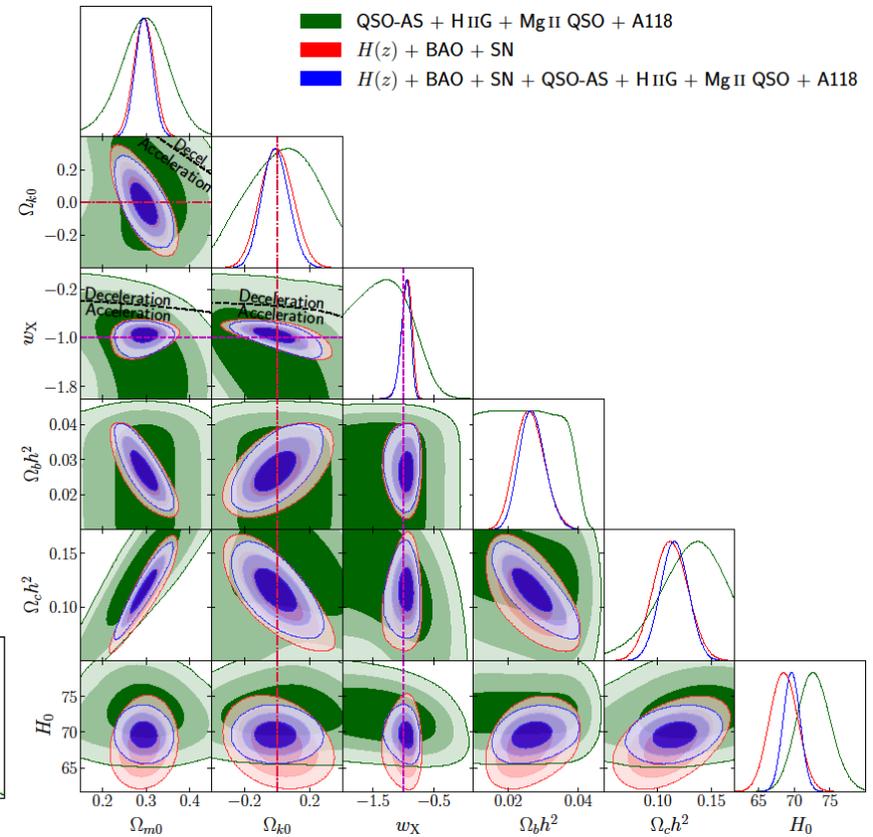


$$\Omega_k = 0.018 \pm 0.059$$

Flat and non-flat Λ CDM



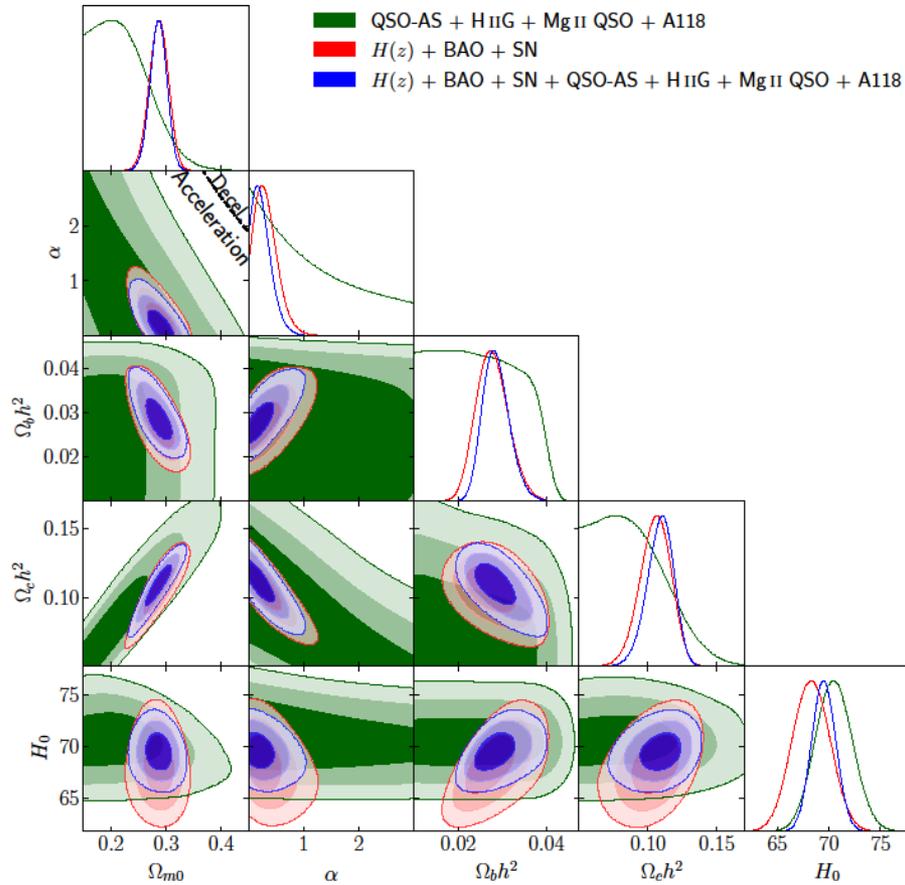
$$w_X = -0.959 \pm 0.059$$



$$\Omega_k = -0.009^{+0.077}_{-0.083}$$

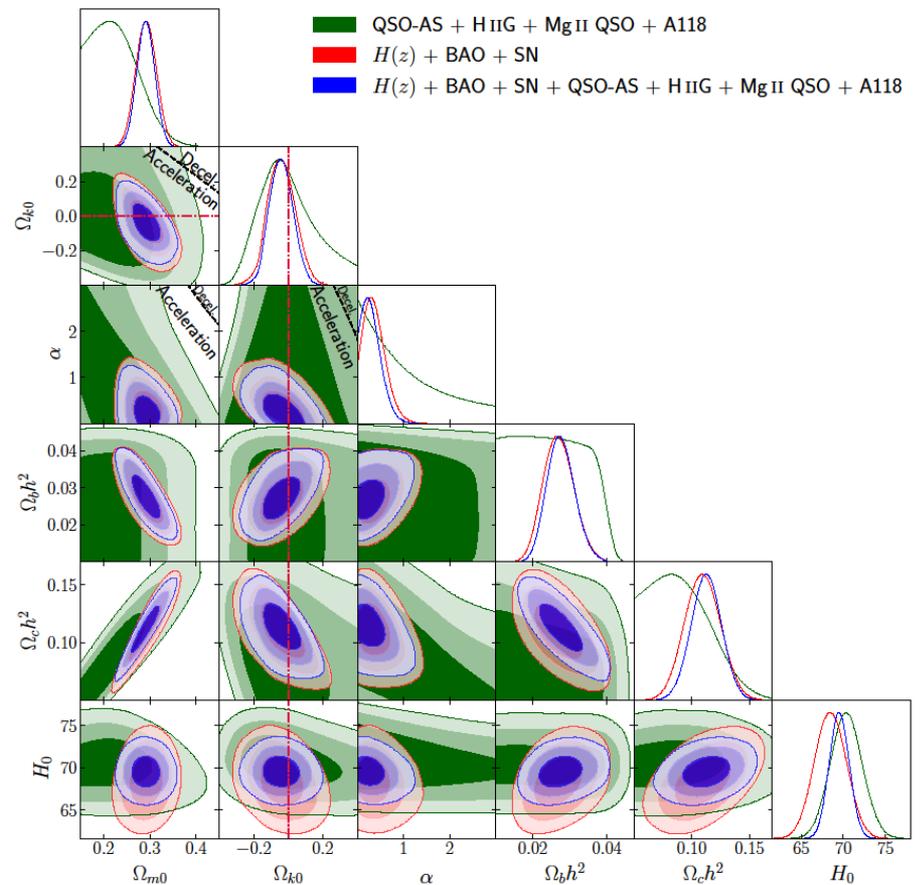
$$w_X = -0.959^{+0.090}_{-0.063}$$

Flat and non-flat ϕ CDM



$$\alpha = 0.249^{+0.069}_{-0.239}$$

1.0 σ dynamical DE



$$\Omega_k = -0.040^{+0.064}_{-0.072} \quad \alpha = 0.316^{+0.101}_{-0.292}$$

1.1 σ DDE

Do observations really require close to zero space curvature?

Including CMB anisotropy data requires first figuring out how to deal with spatial inhomogeneities and the appropriate $P(k)$.

In **spatially-flat** case $P(k) \sim k^n$ where n is spectral index.

In closed model (open is similar), eigenvalue of spatial Laplacian = $-A(A+2)$ where $A = 2, 3, 4, \dots$ and $q \sim A + 1$.

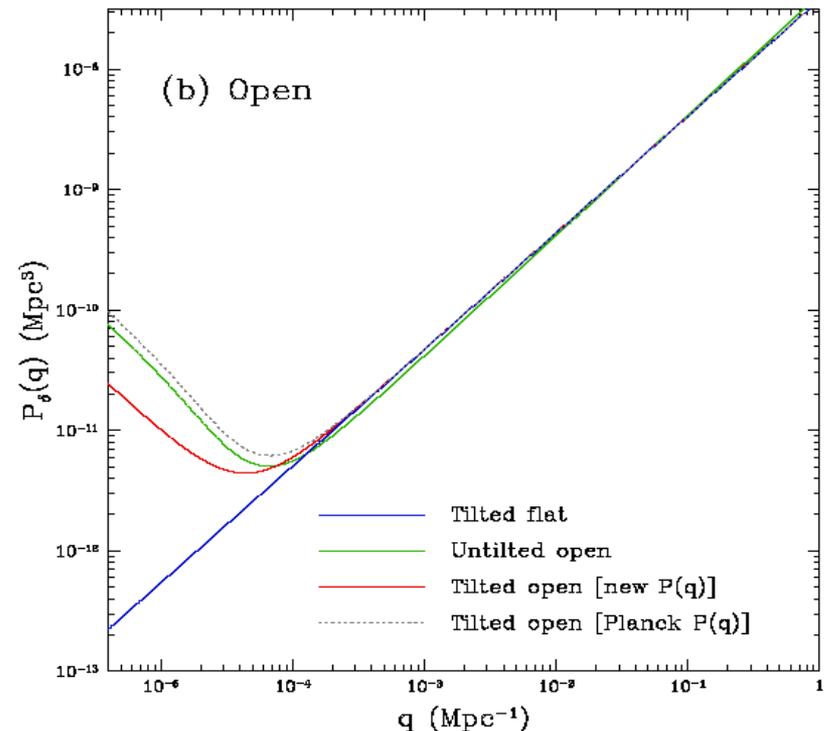
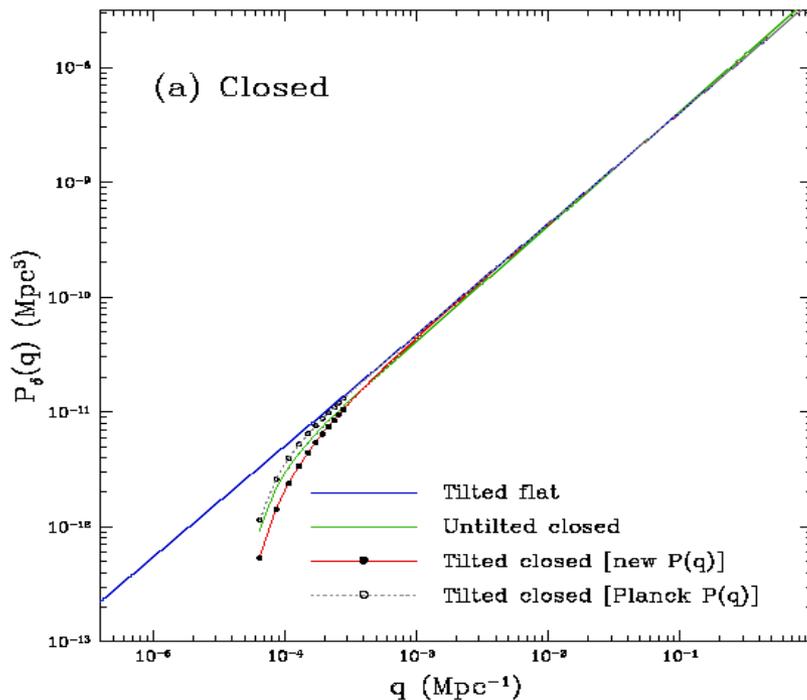
Slow roll inflation gives in **non-flat models** (Ratra & Peebles PRD52, 1837 (1995), Ratra PRD96, 103534 (2017)) $P(q) \sim (q^2 - 4K)^2 / [q (q^2 - K)]$ where spatial curvature $K = -H_0^2 \Omega_{K0}$. **This was the only known physically consistent $P(k)$ in a non-flat model. It is un-tilted and is a bad fit to Planck CMB data.**

In the non-flat case Planck 2018 and others have added an **arbitrary tilt prescription** to the **un-tilted non-flat** case, “Planck $P(q)$ ” : $P(q) \sim (q^2 - 4K)^2 / [q (q^2 - K)] k^{n-1}$ with $q^2 = k^2 + K$. **Can find closed inflation models that give $P(k)$ that are numerically similar to this (Guth, Namjoo + BR, in preparation).**

For “Planck $P(q)$ ”, P18 data: $\Omega_{K0} = -0.04$ at 2.5σ and P18 + lensing: $\Omega_{K0} = -0.01$ at $1.6\sigma_{11}$

Can also find non-flat inflation models that give “new $P(q)$ ” different from what Planck 2018 assumed (BR PRD106, 123524 (2022)).

Inverse powers of $\sinh(c\varphi)$ and $\cosh(c\varphi)$ inflaton potential energy densities in open and closed models. $\Omega_{K0} = \pm 0.0103$ and other parameters from P18+lensing Planck $P(q)$ analysis (de Cruz, Park + BR 2211.04268).



Data: P18 = TT, TE, EE + low E

(P18) lensing = lensing potential power spectrum

Non-CMB = BAO (16, including $f\sigma_8$) (8) + $f\sigma_8$ (8)
+ SNIa (Pantheon 1048 + DES 3 yr 20 bins) + H(z) (31)

Models (six):

Flat tilted $P(k) \sim k^n$

Non-flat tilted Planck $P(q)$

Non-flat tilted new $P(q)$

without and with phenomenological A_L parameter as there is degeneracy with Ω_{K0} (di Valentino+ NatAst4, 196 (2019)).

$A_L = 1$ inconsistencies	P18 vs lensing	P18 vs non-CMB	All data Ω_{K0}	
Flat $P(k) \sim k^n$	0.72σ	1.7σ	
Non-flat Planck $P(q)$	2.5σ	$3.0\sigma \leftarrow$ Ruled out		
Non-flat new $P(q)$	2.2σ	2.6σ	0.0003 ± 0.0017	Flat
$A_L \neq 1$ consistency	P18 vs non-CMB	All data Ω_{K0}	All data A_L	
Flat $P(k) \sim k^n$	0.84σ	1.089 ± 0.035	2.5σ
Non-flat Planck $P(q)$	0.79σ	-0.0002 ± 0.0017	1.090 ± 0.036	2.5σ
Non-flat new $P(q)$	0.40σ	-0.0002 ± 0.0017	1.088 ± 0.035	2.4σ
Both flat				

Handley (+Lemos) PRD103, L041301 (2021)
 Suspiciousness gaussian approximation, qualitatively consistent with Joudaki et al. MNRAS465, 2033 (2017) DIC statistic.

Consistent with flat geometry, but wants more lensing than standard Λ CDM predicts.

For “Planck P(q)”, P18 data: $\Omega_{K0} = -0.04$ at 2.5σ , P18 + lensing: $\Omega_{K0} = -0.01$ at 1.6σ , non-CMB data: $\Omega_{K0} = -0.03$ at 0.66σ .

For “new P(q)”, P18 data: $\Omega_{K0} = -0.03$ at 2.4σ , P18 + lensing: $\Omega_{K0} = -0.009$ at 1.5σ , non-CMB data: $\Omega_{K0} = -0.04$ at 0.71σ .

This is because of $\Omega_{K0} - \Omega_{m0} - A_L - H_0$ degeneracy.

Non-CMB data favor higher h and lower Ω_{m0} than do P18 and P18 + lensing data. This makes P18+lensing+non-CMB data very consistent with flat geometry even though P18 + lensing data and non-CMB data are both consistent with closed geometry.

The earlier (different) non-CMB data combination I used favors flat geometry.